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ABSTRACT

In this presentation we will investigate the mathematics and physics of a free-falling object, not for the purpose of research to discover some profound physical phenomena, but rather to enhance students' ability to gather, organize, and analyze data using state of the art hand held technology. We will use the TI-83 plus (a sophisticated graphing calculator) and the TI-CBR (a Calculator Based sonic Ranging device) along with an adequate supply of 8 to 12 cup, no special brand, coffee filters. Since the coffee filters are not consumed, a single package is generally sufficient to supply the needs of more than one class. We will use the CBR and TI-83 Plus to collect data about the coffee filter drops. We will manually analyze some of the data and then use a previously written program to expedite the task. From the information obtained during the presentation we should be able to draw a reasonable conclusion about the terminal velocity that we challenge you to verify with your students. (Author)

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COFFEE FILTER TERMINAL VELOCITY

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COFFEE FILTER TERMINAL VELOCITY

INTRODUCTION/OVERVIEW

In this presentation we will investigate the math and physics of a free-falling object, not for the purpose of research to discover some profound physical phenomena, but rather to enhance students' ability to gather, organize, and analyze data using state of the art hand held technology.

We will use the TI-83 plus (a sophisticated graphing calculator) and the TI-CBR (a Calculator Based sonic Ranging device) along with an adequate supply of 8 to 12 cup, no special brand, coffee filters. Since the coffee filters are not consumed, a single package is generally sufficient to supply the needs of more than one class.

We will use the CBR and TI_83 Plus to collect data about the coffee filter drops. We will manually analyze some of the data and then use a previously written program to expedite the task. From the information obtained during the presentation we should be able to draw a reasonable conclusion about the terminal velocity that we challenge you to verify with your students.

$$d = \frac{1}{2}at^2 + v_o t + d_o$$

if $v_o = 0$ initial velocity and $d_o = 0$ initial displacement

then
$$d = \frac{1}{2}at^2$$

Displacement equals one half times acceleration times time squared. Where acceleration is the result of a net force different from zero.

When an object moves through a fluid there is resistance to that movement related to the size of the object projected in the direction of motion (cross-sectional area), the nature of the surface (drag coefficient), the viscosity of the fluid and the speed of the object. This resistance is called Drag Force.

An object free falling in a fluid is subject to acceleration due to the force of gravity as reduced by drag force. When the drag force, which increases with speed, equals the weight of the object no further acceleration occurs and the object is said to be at "Terminal Velocity"

$$F_{\text{terminal drag}} = mg \quad m = \text{mass}, \quad g = 9.8 \text{ Nm/sec}^2$$

For a small object falling through a high viscosity fluid the drag force is directly proportional to the object's velocity.

$$F_{\text{drag}} = kv \quad \text{When} \quad mg = kv \quad \text{then} \quad v_{\text{terminal}} = mg / k$$

For heavier larger cross-sectional area objects free falling in air the drag force is directly proportional to the square of the object's velocity.

$$F_{drag} = Pv^2$$

Where P is proportional to area, drag coefficient and viscosity.

$$\text{When } F_{drag} = mg = Pv^2 \quad \text{then} \quad v^2 = \frac{mg}{P}$$

For coffee filters dropped in groups of 1,2,3, etc., the only variable is the mass, which is proportional to the number of filters.

$$m = M \leftarrow N \quad \begin{array}{l} m = \text{total mass dropped} \\ M = \text{mass of one filter} \\ N = \text{number of filters dropped} \end{array}$$

Area is constant unless the filters are deformed. Drag coefficient is constant. Viscosity is constant.

$$V_{termnlcoffee\ filter} = K \sqrt{N} \quad \text{Where} \quad K = \sqrt{\frac{Mg}{P}}$$

For regular 8-12 cup size, not heavy-duty industrial commercial grade, but the kind you get at K-Mart or WalMart, any brand, We have found that

$$K \cup 1 \quad \text{and so} \quad V_{termnlcoffee\ filter} = \sqrt{N}$$

In this exercise we will attempt to verify this item.

When an object with a large mass to cross-sectional area ratio falls in air its time distance plot is parabolic.

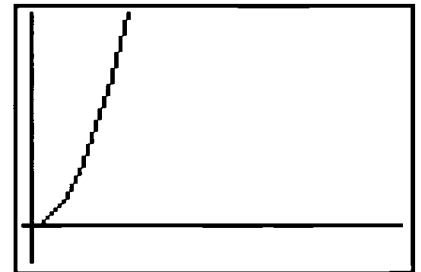
$$d = \frac{1}{2}gt^2 \quad \text{or on the TI 83}$$

```

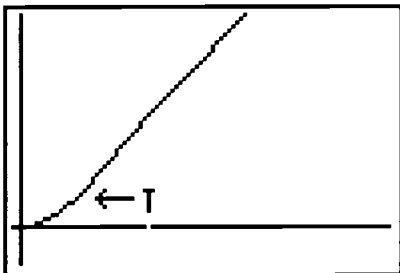
Plot1 Plot2 Plot3
Y1=(1/2)9.8X^2
Y2=
Y3=
Y4=
Y5=
Y6=
Y7=

```

which with this window
 (Xmin,Xmax,Ymin,Ymax)
 (-0.5,1.5,-0.5,5)
 gives this graph



In the case of coffee filters the curve is flattened and becomes linear like this



This complicated curve is assumed to be parabolic until terminal velocity is attained at T then becomes linear. We will, for this exercise, consider this function to be piece wise defined.

For $X = 0$ to T $Y = jX^2$ where j depends on number of filters

For $X > T$ $Y = aX + b$ where a and b depend on number of filters

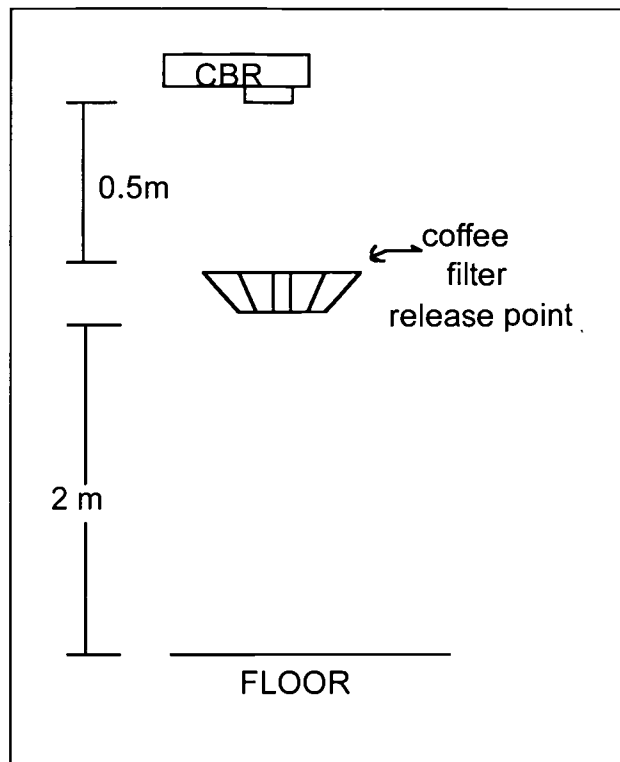
a is the slope of the time distance plot $\text{slope} = \frac{\Delta d}{\Delta t} = \text{velocity}$

-----TERMINAL VELOCITY.

COFFEE FILTER TERMINAL VELOCITY

DATA COLLECTION USING THE TI 83 AND THE CBR

The data collection setup should look something like this...



We have found that teams of at least three students work best for gathering the data. That's one holding the CBR at a height of about 8 foot, one running the TI-83, and one dropping the filters.

As you can see in the drawing the drop point of the filters is about half a meter below the CBR. This is because the device measures range from 0.5 to 6 meters. Drops from any closer will eliminate some of the parabolic time distance data. It should also be noted that the filter is dropped away from the CBR rather than onto it. This is for several very good reasons. The filters fall fairly straight and starting at the CBR rather than trying to land on it is considerably more productive. Additionally if they are dropped on the CBR each set of filters must be moved (if the aim was good) before the next set can be dropped. The time for each drop is somewhat less than 3 seconds so it is not difficult with this setup to get as many as six drops for each 18 second CBR activation. We really want to look at the linear part of the data and the last half meter would be lost because of being too close. We may not even attain linearity before that time for some drops.

DATA COLLECTION PROCEDURE:

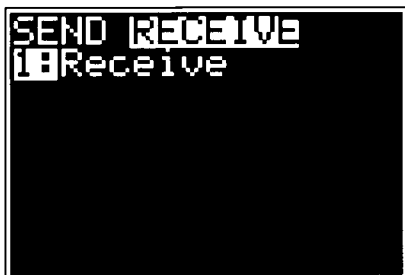
Decide how many filters will be in the drops. Count out and set-aside in at least six separate stacks the filters for the next drop. Care should be taken to insure that the same number of filters is in each stack, as they tend to stick together. Care should also be taken to not deform or flatten the filters in order to favorably compare to other drops.

Get ready to run the RANGER program with the TI83 and CBR
(if your TI 83 already has prgmRANGER skip to ***)

Connect the two units (CBR and TI-83) with the long link cable

Turn on the TI 83 press 2nd LINK to display the Link menu.

Press **1** to select **1 : R e c e i v e**. The message **W a i t i n g ...** is displayed and the busy indicator is on



On the CBR open the hinged portion containing the screen 82/83 press while the **W a i t i n g ...** message is still displayed.

This screen will display

```
Receiving...
▶ RANGER PRGM
Done
```

Go to the home screen (Press)

Then Press twice

Press

This or similar screen will appear

Select #:RANGER press

```
EDIT NEW
1:DROPSTRT
2:MIN
3:PIC
4:RANGER
5:TERMVEL
```

```
PRGM RANGER
```

This is pasted on the home screen ready for execution. Press

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YOU WILL SEE
THESE SCREENS

PLEASE FOLLOW
THESE INSTRUCTIONS

```
TEXAS INSTRUMENTS
RANGER (V1.00)
PRESS [ENTER]
```

Press

[ENTER]

```
MAIN MENU
1: SETUP/SAMPLE
2: SET DEFAULTS
3: APPLICATIONS
4: PLOT MENU
5: TOOLS
6: QUIT
```

Select 2: SET DEFAULTS

Press

[ENTER]

```
MAIN MENU  ▶ START NOW
REALTIME: YES
TIME(S): 15
DISPLAY: DIST
BEGIN ON: [ENTER]
SMOOTHING: NONE
UNITS: METERS
```

Press

[ENTER]

```
POINT CBR
AT TARGET
TO START PRESS
[ENTER] ON T183
```

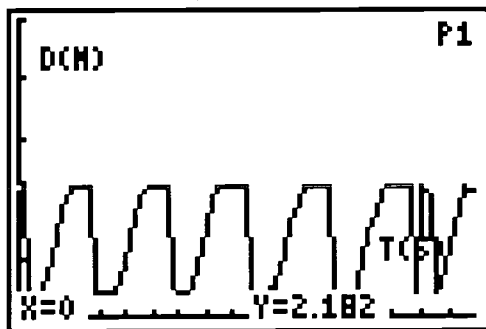
When you are ready to drop filters

Press

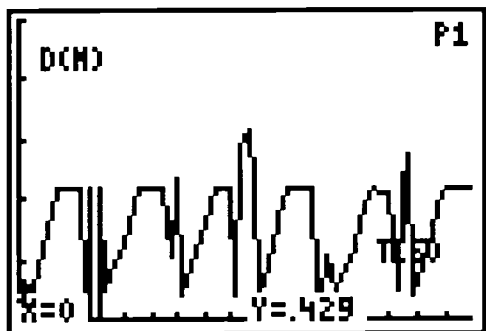
[ENTER]

Lights will flash and bells will ring (not really bells, but rather clicking) while the CBR is actuated to find Time/Distance data.

When the data collection is complete a screen like this will be displayed



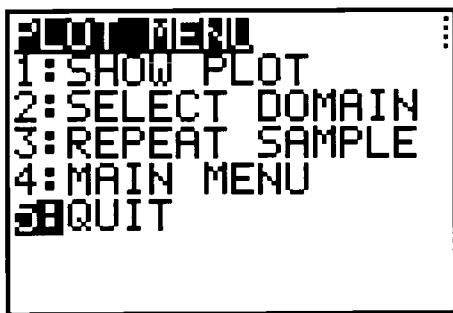
This particular screen is for a good run of six drops of 4 filters



This screen is for an OK run of six drops of 3 filters with some clutter that will not make much difference.

Look at your display and if there is not at least three drops with fairly good data you may want to try again.

Press This screen will appear.



To try again select 3: REPEAT SAMPLE which will take you to the top of the previous page

When you have good data select 5: QUIT

This screen will appear

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```
L1=TIME
L2=DIST
L3=VEL
L4=ACCEL
Done
```

Since we did not do VELOCITY or ACCELERATION, L3 and L4 will be filled with zeros.

From the SETUP/SAMPLE screen you can choose to display VELOCITY or ACCELERATION plots. We found that for this procedure these plots were not productive.

COFFEE FILTER TERMINAL VELOCITY
ANALYZING THE COLLECTED DATA
USING THE TI 83 OR TI 83 PLUS
WITH MANUAL INPUTS AND MANIPULATION

Considering that data was just received by one person, either from the CBR or from the Graph Link we need to share this data with our teammates before we analyze the data. Connect the link cable to both TI 83s.

Press

2nd

LINK

Receiver (needs data)-- scroll over to RECEIVE

```

SEND RECEIVE
1: All+...
2: All-...
3: Prgm...
4: List...
5: Lists to TI82...
6: GDB...
7: Pic...
    
```

```

SEND RECEIVE
1: Receive
    
```

Press

ENTER

Waiting...

Sender (the one that has the data)

Press

2nd

LINK

Select 4:List... Press

ENTER

```

SELECT TRANSMIT
L1 LIST
L2 LIST
L3 LIST
L4 LIST
L5 LIST
L6 LIST
Q LIST
    
```

Mark L1 and L2

Scroll to TRANSMIT

Press

ENTER

This will show on the receiving unit

```
DuplicateName
1:Rename
2:Overwrite
3:Omit
4:Quit

L1      LIST
```

Select 2:Overwrite

Press

ENTER

Then this will show

Select 2:Overwrite

```
DuplicateName
1:Rename
2:Overwrite
3:Omit
4:Quit

L2      LIST
```

Press

ENTER

```
Receiving...
  L1      LIST
  L2      LIST
          Done
```

This process needs to be repeated
so all will have the Time/Distance data.

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We need to save this data so that we can analyze it with out loosing it. To do this we will store the Time/Distance data lists in named lists. Of the many ways to name a list this is the way we choose to proceed.

Go to the home screen (Press **2nd** **QUIT**)

Then Press **CLEAR** twice

Then Press **STAT** select 5:SetUpEditor

```

3000 CALC TESTS
1:Edit...
2:SortA(
3:SortD(
4:ClrList
5:SetUpEditor
  
```

Press **ENTER** twice.

```

SetUpEditor
Done
  
```

Then press **STAT** **ENTER**

```

3000 CALC TESTS
1:Edit...
2:SortA(
3:SortD(
4:ClrList
5:SetUpEditor
  
```

L1	L2	L3	1
0	.88102	0	
.19988	1.0448	0	
.39977	1.2292	0	
.59965	1.3874	0	
.69959	1.4754	0	
.89948	1.6573	0	
1.0994	1.8284	0	
L1(1)=0			

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@@@

move the cursor to the very top of L1 Press

2nd **INS**

	L1	L2	1
	0	.88102	
	.19988	1.0448	
	.39977	1.2292	
	.59965	1.3874	
	.69959	1.4754	
	.89948	1.6573	
	1.0994	1.8284	
Name=			

Type the name of the new list like this

CF1T or CF1D

That's Coffee Filters # Time or Distance

For this example we are dealing with the data for one coffee filter.

We used CF1T for the time data

Press

ENTER

Press

2nd

L1

	L1	L2	1
	0	.88102	
	.19988	1.0448	
	.39977	1.2292	
	.59965	1.3874	
	.69959	1.4754	
	.89948	1.6573	
	1.0994	1.8284	
CF1T=L1			

Press

ENTER

CF1T	L1	L2	1
0	0	.88102	
.19988	.19988	1.0448	
.39977	.39977	1.2292	
.59965	.59965	1.3874	
.69959	.69959	1.4754	
.89948	.89948	1.6573	
1.0994	1.0994	1.8284	
CF1T(1) =			

L1, the time data list, has now been stored in LCF1T.

Go back to @@@ and repeat the process

Storing L2, the distance data list, into LCF1D. Like this.

CF1T	CF1D	L1	2
0	.88102	0	
.19988	1.0448	.19988	
.39977	1.2292	.39977	
.59965	1.3874	.59965	
.69959	1.4754	.69959	
.89948	1.6573	.89948	
1.0994	1.8284	1.0994	
CF1D(1) = .881019			

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If your calculator was used with the CBR then you can view the statistical plot of the data.

Just Press **GRAPH** and show the graph to your teammates.

Now let's all get on the same page.

Press **2nd** **STAT PLOT** Then Press **ENTER**

```



STAT PLOTS
1:Plot1...On
  L1 L2 .
2:Plot2...Off
  L1 L2 ■
3:Plot3...Off
  L1 L2 ■
4↓PlotsOff
  
```

becomes

```

Plot1 Plot2 Plot3
Off Off Off
Type: L1 L2 L3
Xlist:L1
Ylist:L2
Mark: ■ + ■
  
```

but it may not look like this. Move the cursor to highlight an item

Then Press **ENTER**
 highlight **On** , connected dots  , make **Xlist:L1** and
Ylist:L2 
 and highlight the dot

Press **Y=**

```

Plot1 Plot2 Plot3
Y1=
Y2=
Y3=
Y4=
Y5=
Y6=
Y7=
  
```

By highlighting and clearing
 make the screen look like this

Press **WINDOW**

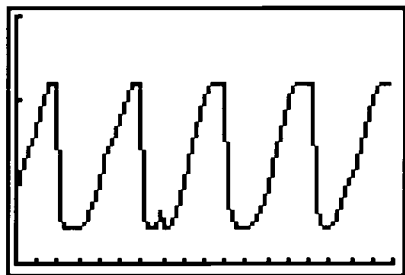
```

WINDOW
Xmin=0
Xmax=18
Xscl=1
Ymin=0
Ymax=3
Yscl=1
Xres=1
  
```

Make the screen look like this

Press

GRAPH

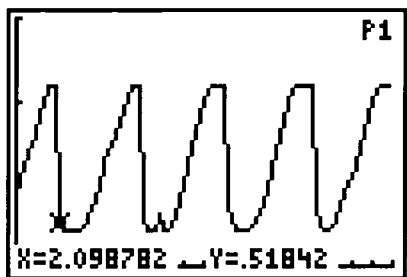


This is a Time/Distance plot of collected data. From this mentally choose a filter drop to analyze. You may get together with your team and choose different drops. Determine the start time of that drop by using the Xscale = 1sec for each mark. I will look at the second of my drops which starts at about 2 seconds.

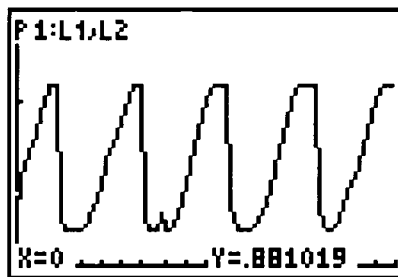
Press

TRACE

and scroll to the beginning of the chosen drop



becomes



Press

WINDOW

and put an X for Xmin= X

Press

ENTER

```
WINDOW
Xmin=X
Xmax=18
Xscl=1
Ymin=0
Ymax=3
Yscl=1
Xres=1
```

becomes with your value of X

Put Xmax=X+4

Press

ENTER

```
WINDOW
Xmin=2.098782
Xmax=18
Xscl=1
Ymin=0
Ymax=3
Yscl=1
Xres=1
```

```
WINDOW
Xmin=2.098782
Xmax=X+4
Xscl=1
Ymin=0
Ymax=3
Yscl=1
Xres=1
```

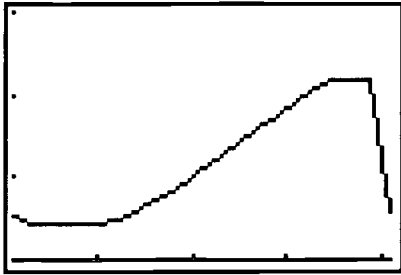
becomes with your value of X+4

```
WINDOW
Xmin=2.098782
Xmax=6.098782
Xscl=1
Ymin=0
Ymax=3
Yscl=1
Xres=1
```

Press

GRAPH

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This is the Time/Distance plot for the chosen drop. It should clearly show the linear part where the filter has attained terminal velocity. To have the calculator determine the slope of this line we will select just the linear part. To see this more clearly


Press

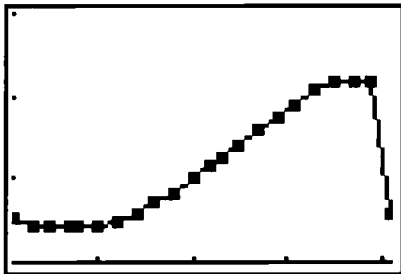
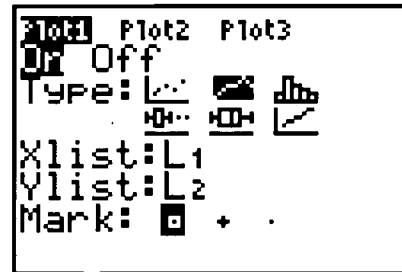
2nd

STAT PLOT

Then Press

ENTER

select the dark block around the dot 



Press

2nd

LIST

Scroll over to **OPS** down to **8:Select (**

```
NAMES OPS MATH
6: ↑cumSum(
7: ↑List(
8: Select(
9: ↑augment(
0: List→matr(
A: Matr→list(
B: L
```

Press

ENTER

Select (is pasted to the home screen.

Press **2nd** L3 then, then **2nd** L4 then)

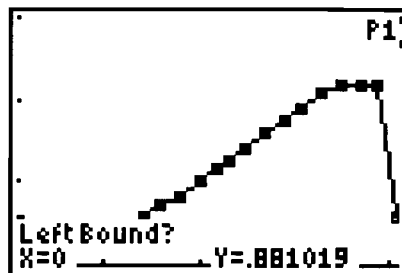
then Press

ENTER

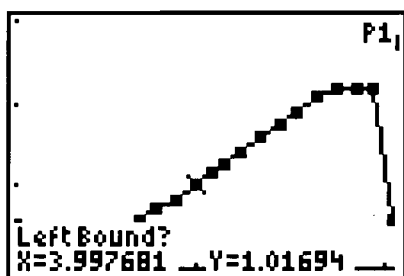
BEST COPY AVAILABLE

Select(L3,L4)

becomes



Move the marker to the right until at the start of the linear part of the graph (the left bound). Keep in mind that you are starting at the beginning of the CBR Time/Distance lists and the marker may not be in sight for some time.



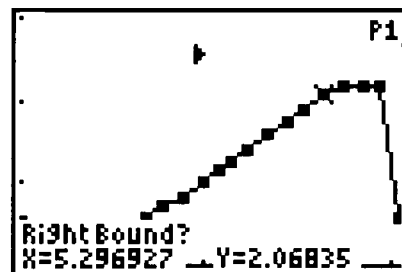
Press

ENTER

Move the marker to the right bound.

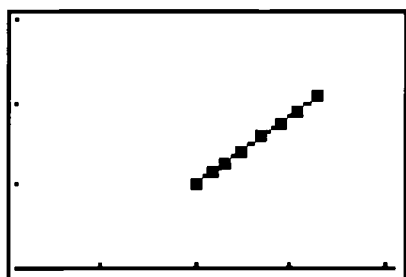
Press

ENTER



=

What is now displayed is the linear part that you selected in the same window you had. These data points are now stored in L3 and L4 .



To find the slope of this discrete data we will do a linear regression.

Press

STAT

and down to

scroll right to CALC
4:LinReg(ax+b)

Press

ENTER

```

EDIT  [F1]  TESTS
1:1-Var Stats
2:2-Var Stats
3:Med-Med
4:LinReg(ax+b)
5:QuadReg
6:CubicReg
7:QuartReg
  
```

LinReg(ax+b) is pasted to the home screen

we must enter the arguments L3,L4,Y1

(Y1 is found in VARS → Y-VARS

1:FunctionHighlight 1:Y1 and press

ENTER to paste the home screen)

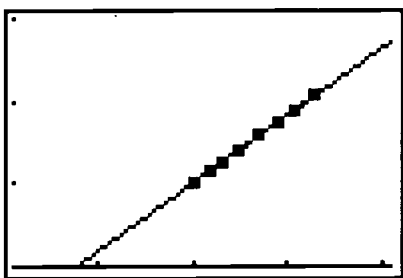
```
LinReg(ax+b) L3,  
L4,Y1
```

Press ENTER
The TI-83 will perform the regression, display it and paste the equation at Y1
=
“a” is the slope and
TERMINAL VELOCITY

```
LinReg  
y=ax+b  
a=.8148136572  
b=-2.250644492
```

for this drop
Press

GRAPH



Using our data the TERMINAL VELOCITY of the second drop of one filter was .815 m/s.

COFFEE FILTER TERMINAL VELOCITY
ANALYZING THE COLLECTED DATA
USING THE TI 83 OR TI 83 PLUS
(ANALYZING ASSIST PROGRAM)

“TERMVEL”

The TI 83 Plus program was written to assist in analyzing the coffee filter time distance data. The intent is to remove the repetitious button punching necessary to analyze many coffee filter drops to provide a reasonable data base for more in-depth analysis while maintaining some uniformity in processing techniques. The program asks the user for the raw Time/Distance data lists as provided by the CBR and leads the user through a series of screens to arrive at the Terminal Velocity of a particular coffee filter drop.

The coffee filter drops and the CBR ranging pulse are non-synchronous, therefore this program uses a best guess at the shape of the nonlinear portion of the drop and from that provides only a close approximation of the distance of fall before terminal velocity is reached.

These two pieces of data are automatically stored in two TI 83 matrices for later evaluation. Matrix A and B have 13 rows for 1 through 12 filter drops and a 15 filter drop and 7 columns for six trials and an average for each number of filters dropped.. Terminal velocity is stored in Matrix A and drop distance to terminal velocity in Matrix B.

The program uses the six calculator lists L1-L6. Collected data need be stored elsewhere (see the instructions for manually analyzing data page 10).

Smoothing with this program is for the specific elimination of single bits of extraneous data and not overall smoothing like the CBR does. With CBR smoothing data bits are lost and misleading information may result.

To use the program follow the instructions found on page 45 to load the program into your calculator.

For those of you at the presentation we will link the program to you for use and retention if you want.

***Press

PRGM

This or similar screen will appear

Select #:TERMVEL press

ENTER

```
EDIT NEW
1: DROPSTRT
2: MIN
3: PIC
4: RANGER
5: TERMVEL
```

PRGMTERMVEL

This is pasted on the home screen ready for execution. Press

ENTER

YOU WILL SEE
THESE SCREENS

PLEASE FOLLOW
THESE INSTRUCTIONS

```
A PROGRAM FOR :
PROCESSING
COFFEE FILTER
VELOCITY
W. CAUDILL
S. PARKER
MEQVSD MPCC
ZANESVILLE OHIO
```

Press

ENTER

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```
THIS PROGRAM WILL  
SAVE ORIGINAL  
DATA IN L5,L6  
THEN LISTS L1-L4  
WILL BE USED FOR  
PROCESSING
```

Press

ENTER

```
TIME LIST =
```

Insert the name of the list containing the time data. You can not just type it in without the list identifier character. It is best to

Press

2nd

LIST

Then select the desired list.

Then Press

ENTER

For this demonstration we will use the data from five coffee filters dropped . These lists are stored in our LCF5T and LCF5D.

```
TIME LIST =LCF5T  
DISTANCE LIST =
```

Same as above for time list.

Then Press

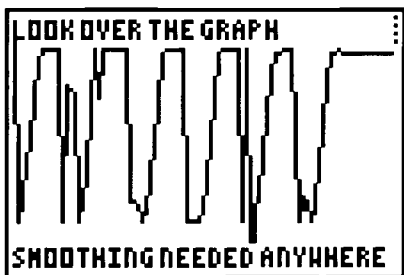
ENTER

```
TIME LIST =LCF5T  
DISTANCE LIST =L  
CF5D  
NØ. OF FLTRS =  
IN THIS DROP?
```

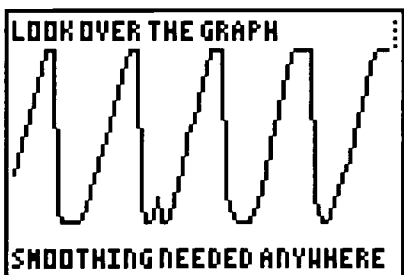
Input the number of filters dropped for the data you are using. We used 5.

Then Press

ENTER



This is very much like the CBR Time/Distance plot. The question that is being asked is about inconsistent data. In this case the second drop and the fifth drop may have some “where did that come from” data.



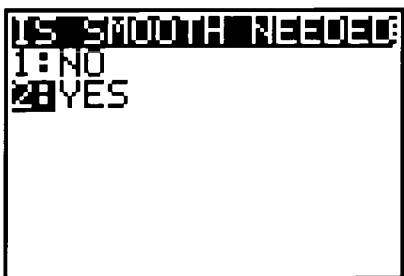
This display is our data for one-filter drops and there appears to be no significant extraneous data.

Look over your display with this in mind.

Then Press

ENTER

(We returned to the five filter drop)



Let us all Press 2

to see what the smoothing is about.



The numbers across the middle of the screen are time in seconds from 0 to 18. Decide which drop to consider and note the time just a little left of its start.

Then Press

ENTER

START TIME?

Input the time you just noted on the previous screen. (We will look at our 2nd drop which starts at 2 seconds.)

Then Press

ENTER

START TIME?2
DROP NUMBER?

Input the number of the drop you are considering. (Ours is number 2)

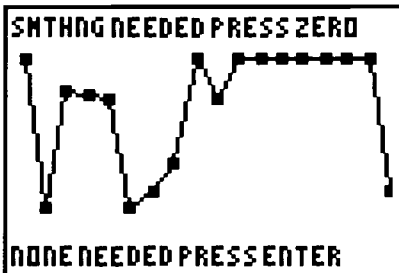
Then Press

ENTER

PLEASE WAIT

Please wait

This screen shows the extraneous data at the start of the drop and in the

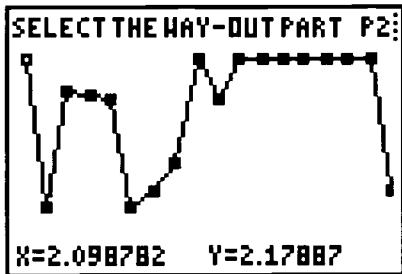


linear portion. The start is best guess anyway so that part in this case can be ignored. The data showing just below the last D in NEEDED ;however, will keep the linear portion of this drop from being realistic and should be eliminated. We will press 0. If no smoothing is needed (a judgment call) then

Press

ENTER

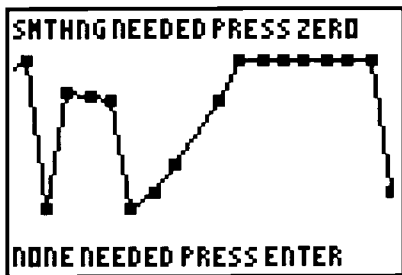
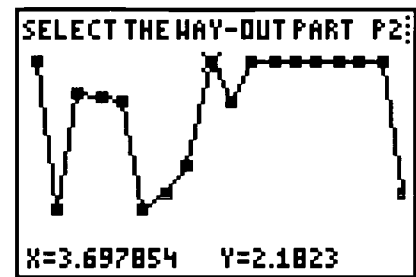
If you pressed ENTER you will skip to \$\$\$\$ if not then



Move the marker to the extraneous data.

Press

ENTER



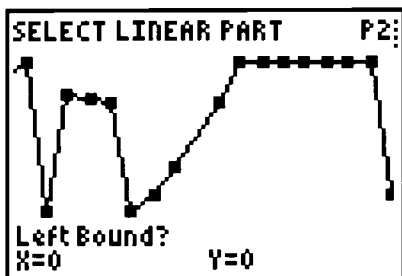
The extraneous data has been eliminated and you are asked if more smoothing is needed.

If more is needed press 0 and eliminate those points also. Otherwise

Press

ENTER

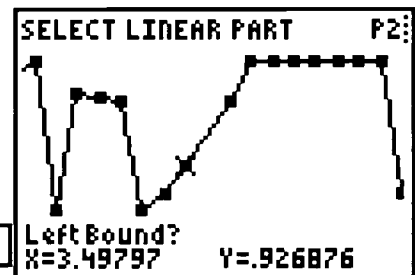
\$\$\$\$



Move the maker to the left edge of the linear part and then

Press

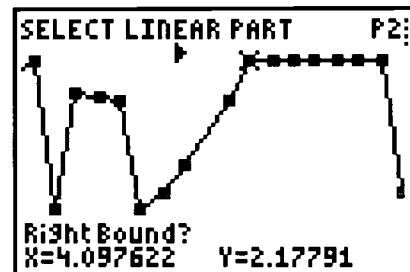
ENTER

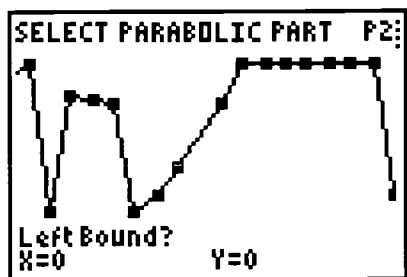


Move the marker to the right end (bottom) of the linear part and

Press

ENTER

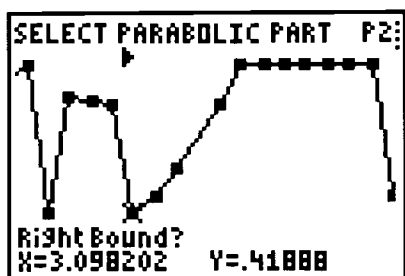
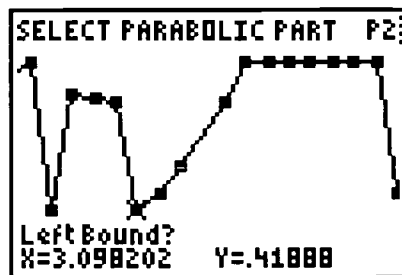




move the marker to the left (beginning) of the drop parabolic part

Press

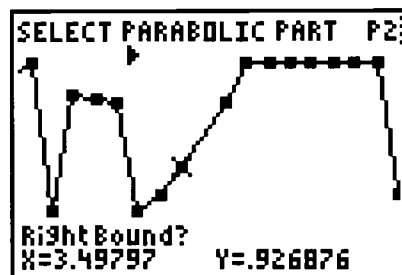
ENTER



Move the marker to the end of the parabolic part (start of the linear part). You must have at least three data points.

Press

ENTER



NUMBER OF CF
TREMVEL NOW
AVG TERMVEL
THIS DROP
AVG DROP

This display shows the processed terminal velocity for this drop and the average of the other drops that have been processed, as well as the distance to reach terminal velocity for this and the average of the processed drops for this number of filters

BEST COPY AVAILABLE

```
DO ANOTHER DROP?
1: YES
2: NO
```

Press

ENTER

The program returns to this screen for you to process another drop

```
DROPS DONE 2
01234567890123
```

COFFEE FILTER TERMINAL VELOCITY

COLLECTED DATA
USING THE TI 83 AND THE CBR

COFFEE FILTER CBR DATA

This file contains the data collected with a CBR at Mid-East Ohio Vocational School, Mushingum Perry Career Center, Zanesville, Ohio.

This is empirical data and will have the same inaccuracies that you would get with your students gathering data. The setup is as shown in the previous sections.

In order to use this data in a TI 83 it must be converted into a ***.8xl** file. To do this, select a single column, title and all. Open TI-Graph Link and open a File: New TI-83 List File. Paste the column onto the new list form. Select (high light) the title, cut it and past it to the "Name:" box.

The list can be imported into the TI-83 or saved for later use.

The data can be analyzed manually or by using the TI-83 Plus program TERMVEL.

NOTE: There is not enough space to put all these lists in the TI-83 at the same time unless some of it is put into archives. To process a drop both a time and a distance list are needed.

CF1T	CF1D	CF2T	CF2D	CF3T	CF3D	CF4T	CF4D
0	0.88101	0	0.42025	0	0.42931	0	2.18216
	9		7				
0.19988	1.04481	0.19988	0.41929	0.19988	0.63992	0.19988	2.18216
4		4	6	4	9	4	
0.39976	1.2292	0.39976	0.53270	0.29982	0.41888	0.39976	0.42039
8		8	2	6		8	
0.59965	1.38736	0.49971	0.60437	0.49971	0.57059	0.59965	0.41915
2					5	2	9
0.69959	1.47537	0.69959	0.82115	0.69959	0.84751	0.79953	0.42094
4		4	9	4	9	6	4
0.89947	1.65729	0.89947	1.0444	0.89947	1.15369	0.89947	0.49247
8		8		8		8	5
1.09936	1.82836	1.09936	1.27561	1.09936	1.49363	1.09936	0.71667
2		2		2		2	7
1.29924	1.99435	1.29924	1.52644	1.29924	1.84936	1.29924	1.02889
6		6		6		6	
1.49913	2.17324	1.49913	1.7836	1.49913	2.17283	1.49913	1.38036
1.69901	2.17503	1.69901	2.0045	1.69901	2.17434	1.69901	1.81518

4		4		4		4	
1.89889	2.17104	1.89889	2.18107	1.89889	2.17365	1.89889	2.1429
8		8		8		8	
2.09878	0.51842	2.09878	2.18189	2.09878	2.17379	2.09878	2.17008
2		2		2		2	
2.29866	0.41888	2.29866	2.18422	2.29866	2.17365	2.29866	2.16734
6	4	6		6		6	
2.49855	0.41737	2.49855	0.41792	2.49855	0.43961	2.49855	2.16995
	4						
2.69843	0.41970	2.69843	0.44634	2.69843	2.14057	2.69843	2.16995
4	8	4	3	4		4	
2.79837	0.41957	2.89831	1.66566	2.89831	-2.76033	2.89831	0.42025
7	1	8		8		8	
2.99826	0.41861	3.09820	0.41696	3.09820	2.2115	3.09820	0.41682
1		2		2		2	
3.19814	0.46240	3.19814	0.43302	3.29808	0.44895	3.29808	0.42080
5	7	5		6		6	7
3.39802	0.56222	3.39802	0.58789	3.49797	0.68317	3.49797	0.41764
9		9	5		7		9
3.59791	0.72477	3.59791	0.80797	3.69785	0.97054	3.59791	0.41984
3	8	3	9	4		3	6
3.79779	0.84120	3.79779	1.04907	3.89773	1.28165	3.79779	0.60244
7	4	7		8		7	8
3.99768	1.01694	3.99768	1.30609	4.09762	1.62049	3.99768	0.90532
1		1		2		1	1
4.19756	1.16124	4.19756	1.58795	4.29750	1.92844	4.19756	1.27945
5		5		6		5	
4.29750	1.25323	4.39744	1.87462	4.49739	2.16747	4.39744	1.66003
7		9				9	
4.49739	1.40384	4.59733	2.14702	4.69727	2.17461	4.59733	2.0391
1		3		4		3	
4.69727	1.58095	4.79721	2.17214	4.89715	2.16734	4.79721	2.17338
5		7		8		7	
4.89715	1.73692	4.99710	2.17969	5.09704	2.16665	4.99710	2.17777
9		1		2		1	
5.09704	1.904	5.19698	2.17969	5.29692	2.16651	5.19698	2.17695
3		5		6		5	
5.29692	2.06835	5.39686	0.41847	5.49681	2.17338	5.39686	2.17434
7		9				9	
5.49681	2.17777	5.59675	0.42300	5.69669	1.0639	5.59675	2.17434
1		3	3	4		3	
5.69669	2.18285	5.79663	0.42094	5.89657	2.34033	5.79663	0.43796
5		7	4	8		7	
5.89657	2.17777	5.99652	0.44153	6.09646	0.42231	5.99652	0.4171
9		1	8	2		1	
6.09646	0.58075	6.09646	0.52995	6.29634	0.63169	6.19640	0.41888
3		3	6	6	2	5	4
6.29634	0.41833	6.29634	0.70912	6.49623	0.88472	6.29634	0.42231

7		7	6		6	7	7
6.49623	0.41723	6.49623	0.93415	6.69611	1.17291	6.49623	0.58858
1	7	1	3	4		1	1
6.69611	0.45087	6.69611	1.19419	6.79605	1.33505	6.69611	0.87209
5	4	5		7		5	5
6.89599	0.64583	6.89599	1.45052	6.99594	1.64671	6.89599	1.17058
9	3	9		1		9	
6.99594	0.42176	7.09588	1.71783	7.19582	1.96455	7.09588	1.53029
2		3		5		3	
7.19582	0.41902	7.29576	1.99558	7.39570	2.17695	7.29576	1.89508
6	2	7		9		7	
7.39571	0.48506	7.49565	2.16967	7.59559	2.16967	7.49565	2.15965
	1	1		3		1	
7.59559	0.62674	7.69553	2.17667	7.79547	2.16514	7.69553	2.16638
4	9	5		7		5	
7.79547	0.82019	7.89541	2.16981	7.99536	2.15608	7.89541	2.16336
8	8	9		1		9	
7.99536	0.99195	8.09530	0.4208	8.19524	0.42753	8.09530	2.1639
2		3		5		3	
8.19524	1.17936	8.29518	0.42190	8.39512	2.8766	8.29518	2.16679
6		7	5	9		7	
8.29518	1.26229	8.49507	0.41929	8.59501	3.1439	8.49507	2.16706
8		1	6	3		1	
8.49507	1.45285	8.69495	0.41723	8.79489	2.24916	8.69495	0.50222
2		5	7	7		5	
8.69495	1.63848	8.79489	0.45952	8.99478	0.41806	8.89483	0.41888
6		8	4	1		9	
8.89484	1.82424	8.99478	0.66093	9.19466	0.61961	9.09472	0.41861
		2	6	5		3	
9.09472	2.01576	9.19466	0.88568	9.39454	0.92001	9.29460	0.41751
4		6	7	9		7	2
9.29460	2.16404	9.39455	1.14325	9.59443	1.28137	9.49449	0.44346
8				3		1	
9.49449	2.1672	9.59443	1.4026	9.79431	1.61184	9.59443	0.53901
2		4		7		4	8
9.69437	2.17146	9.79431	1.69765	9.99420	1.99407	9.79431	0.81003
6		8		1		8	8
9.89426	2.17557	9.99420	1.97361	10.1940	2.16555	9.99420	1.132
		2		8		2	
10.0941	0.70336	10.1940	2.16555	10.3939	2.15388	10.1940	1.52384
4		9		7		9	
10.2940	0.52927	10.3939	2.15608	10.5938	2.16665	10.3939	1.90963
3		7		5		7	
10.4939	0.43467	10.5938	2.17049	10.7937	2.16596	10.5938	2.1602
1	3	5		4		5	
10.6938	0.41902	10.7937	0.43838	10.9936	2.15937	10.7937	2.16981
	2	4		2		4	
10.7937	0.42066	10.9936	0.41861	11.1935	0.42478	10.9936	2.16912

4	9	2				2	
10.9936	0.41778	11.1935	0.42012	11.3933	0.43357	11.1935	2.16953
2	6	1		9	5	1	
11.1935	0.42025	11.3933	0.41847	11.5932	1.07116	11.3933	2.16967
1	7	9	3	7		9	
11.3933	0.50565	11.5932	0.52542	11.8931	0.41902	11.5932	2.16967
9	5	7	5			7	
11.5932	0.62592	11.6932	0.61494	11.9930	0.46597	11.7931	0.47503
7	5	2	2	4		6	
11.7931	0.79287	11.8931	0.82390	12.1929	0.68592	11.9930	0.41696
6	6		5	3	3	4	
11.9930	0.95200	12.0929	1.06431	12.3928	0.97026	12.1929	0.42382
4	1	8		1		3	7
12.1929	1.12513	12.2928	1.34782	12.5926	1.29496	12.3928	0.4171
3		7		9		1	
12.2928	1.20984	12.4927	1.59125	12.7925	1.62955	12.5926	0.53338
7		5		8		9	9
12.4927	1.39821	12.6926	1.85609	12.9924	1.97183	12.6926	0.65256
5		4		6		4	1
12.6926	1.5723	12.8925	2.10967	13.1923	2.12889	12.8925	0.96875
4		2		5		2	
12.8925	1.77069	13.0924	2.17695	13.3922	2.13864	13.0924	1.35071
2				3			
13.0924	1.96071	13.2922	2.15814	13.5921	2.13384	13.2922	1.73719
		9		1		9	
13.2922	2.15004	13.4921	0.42204	13.792	2.13164	13.4921	2.11091
9		7				7	
13.4921	2.1569	13.6920	0.42039	13.9918	2.12436	13.6920	2.14661
7		6		8		6	
13.6920	2.16789	13.8919	0.42382	14.1917	0.4359	13.8919	2.14715
6		4	7	7		4	
13.8919	2.17036	14.0918	0.42121	14.3916	2.19878	14.0918	2.14688
4		2	8	5		2	
14.0918	2.16775	14.2917	0.44895	14.5915	2.71267	14.2917	2.14935
2		1	2	3		1	
14.2917	0.69086	14.3916	0.5257	14.7914	0.41874	14.4915	2.14729
1		5		2		9	
14.4915	0.4959	14.5915	0.76775	14.9913	0.61274	14.6914	2.14715
9		3	1		5	8	
14.6914	0.41833	14.7914	0.98028	15.1911	0.89076	14.8913	0.42465
8	5	2		9		6	
14.8913	0.41970	14.9913	1.23263	15.3910	1.18197	15.0912	2.20372
6	8			7		4	
14.9913	0.42218	15.1911	1.46425	15.5909	1.51024	15.2911	1.98199
		9		5		3	
15.1911	0.48657	15.3910	1.71756	15.7908	1.84579	15.4910	0.41915
9	1	7		4		1	
15.3910	0.59036	15.5909	1.96071	15.9907	2.12615	15.6909	0.58212

7	6	5	2	8			
15.5909	0.74056	15.7908	2.14963	16.1906	2.1613	15.8907	0.89063
6	7	4	1	8			
15.7908	0.89914	15.9907	2.17461	16.3904	2.16734	16.0906	1.24197
4	2	2	9	6			
15.9907	1.07076	16.1906	2.17503	16.5903	2.17132	16.1906	1.41935
2	1	7	1				
16.1906	1.25831	16.3904	2.17599	16.7902	2.1742	16.3904	1.81888
1	9	6	9				
16.3904	1.45862	16.5903	2.17571	16.9901	2.17173	16.5903	2.16281
9	7	4	7				
16.5903	1.63257	16.7902	2.17585	17.1900	2.17173	16.7902	2.12697
8	6	3	6				
16.7902	1.81257	16.9901	2.17832	17.3899	2.17187	16.9901	2.12162
6	4	1	4				
16.9901	2.0089	17.1900	2.17859	17.5897	2.17214	17.1900	2.12148
4	3	9	3				
17.1900	2.14812	17.3899	2.17873	17.7896	2.17187	17.3899	2.12175
3	1	8	1				
17.3899	2.1845	17.5897	2.17901	17.9895	2.17228	17.5897	2.12148
1	9	6	9				
17.5898	2.16102	17.7896	2.17859	18.1894	2.17214	17.7896	2.12189
	8	5	8				
17.7896	2.17077	17.9895	2.17612	18.3893	2.17214	17.9895	2.12175
8	6	3	6				

CF5T	CF5D	CF6T	CF6D	CF7T	CF7D	CF8T	CF8D
0	2.3725	0	2.18203	0	0.42259	0	0.42451
0.19988	0.41778	0.19988	2.18189	0.19988	0.41915	0.19988	0.41764
4	6	4	4	4	9	4	9
0.39976	0.65681	0.39976	2.18189	0.29982	0.41888	0.29982	0.42478
8	7	8	6	4	6	8	
0.59965	1.02587	0.59965	2.18189	0.49971	0.47366	0.49971	0.71914
2	2	5	9				
0.69959	1.22659	0.79953	2.18175	0.69959	0.77145	0.69959	1.15492
4	6	4	8	4			
0.89947	1.6706	0.99942	2.18189	0.89947	1.14998	0.89947	1.59084
8	8	8					
1.09936	2.08949	1.19930	2.18189	1.09936	1.59399	1.09936	2.10803
2	4	2	2				
1.29924	2.17832	1.39918	2.18862	1.29924	2.07411	1.29924	2.17118

6	8	6	6				
1.49913	2.18244	1.59907	2.21937	1.49913	2.17448	1.49913	2.1812
	2						
1.69901	2.18216	1.79895	2.30616	1.69901	2.17173	1.69901	2.17901
4	6	4	4	4			
1.89889	2.17859	1.99884	0.4208	1.89889	2.17187	1.89889	2.1812
8			8	8			
2.09878	2.17887	2.19872	0.71626	2.09878	2.17173	2.09878	0.44593
2	4	5	2	2			
2.29866	0.42053	2.39860	1.10714	2.29866	2.17187	2.29866	0.42025
6	8	6	6	6			
2.49855	1.78854	2.59849	1.57175	2.49855	0.43728	2.49855	0.42437
	2						6
2.69843	1.75985	2.79837	2.04089	2.69843	0.42039	2.69843	0.51663
4	6	4	4	4			9
2.89831	1.71124	2.99826	2.1775	2.89831	0.42066	2.89831	0.86262
8			8	9	8		2
3.09820	0.41888	3.19814	2.18065	3.09820	0.42753	3.09820	1.37006
2	4	2	4	2			
3.29808	0.61590	3.39802	2.18079	3.19814	0.54807	3.29808	1.88506
6	3	8	5	9	6		
3.49797	0.92687	3.59791	2.17846	3.39802	0.87978	3.49797	2.16281
	6	2	9	4			
3.69785	2.1823	3.79779	2.1775	3.59791	1.36306	3.69785	2.16226
4	6	3	4				
3.89773	1.67843	3.99768	0.42437	3.79779	1.8716	3.89773	2.172
8		7		8			
4.09762	2.17791	4.19756	0.42053	3.99768	2.16267	4.09762	2.16047
2	4	1	2				
4.29750	2.1753	4.39744	0.41655	4.19756	2.1856	4.29750	2.15745
6	8	5	6				
4.49739	2.17585	4.59733	0.41874	4.39744	2.1856	4.49739	0.42025
	2	7	9				
4.69727	2.17557	4.79721	0.42657	4.59733	2.18532	4.69727	0.41723
4	6	3	3	4			7
4.89715	2.17571	4.89715	0.52240	4.79721	2.1856	4.89715	0.42121
8	8	5	7	8			8
5.09704	2.17928	5.09704	0.85562	4.99710	0.59077	5.09704	0.73136
2	2	1	2				8
5.29692	2.18134	5.29692	1.2929	5.19698	0.43604	5.19698	0.92193
6	6	5	5	5			3
5.49681	0.61562	5.49681	1.71577	5.39686	0.42039	5.39686	1.39821
		9	5	9			
5.69669	0.59366	5.69669	2.17022	5.59675	0.41888	5.59675	1.9548
4	4	3	4	3			
5.89657	0.57389	5.89657	2.18642	5.69669	0.54450	5.79663	2.16363
8	1	8	5	9	7		
6.09646	0.42094	6.09646	2.1683	5.89657	0.85671	5.99652	2.1672

2	4	2	9	8	1		
6.19640	0.53270	6.29634	2.15731	6.09646	1.30389	6.19640	2.16679
5	2	6	3			5	
6.39628	0.85191	6.49623	2.15429	6.29634	1.81655	6.39628	2.1672
9	3		7			9	
6.59617	1.24046	6.69611	2.15457	6.49623	2.16047	6.59617	2.16761
3		4	1			3	
6.79605	1.65152	6.89599	0.50675	6.69611	2.15635	6.79605	0.42053
7		8	5			7	
6.99594	2.11324	7.09588	0.42286	6.89599	2.15663	6.99594	0.41696
1		2	9			1	
7.19582	2.15979	7.29576	0.41778	7.09588	2.15731	7.19582	0.41874
5		6	6	3		5	7
7.39570	2.15841	7.49565	0.41861	7.29576	2.15704	7.39570	0.55288
9			7			9	4
7.59559	2.15828	7.59559	0.41641	7.49565	0.4197	7.59559	0.89790
3		3	3	1		3	7
7.79547	2.15828	7.79547	0.47737	7.69553	0.4171	7.79547	1.35263
7		7	2	5		7	
7.99536	2.15814	7.99536	0.78189	7.89541	0.42080	7.89541	1.5896
1		1	2	9	7	9	
8.19524	0.41778	8.19524	1.1703	8.09530	0.43371	8.09530	2.11681
5		5		3	2	3	
8.39512	0.41888	8.39512	1.61843	8.19524	0.55055	8.29518	2.15745
9		9		6		7	
8.59501	0.41861	8.59501	2.0888	8.39513	0.88445	8.49507	2.1613
3		3			2	1	
8.79489	0.41806	8.79489	2.16651	8.59501	1.39739	8.69495	2.16445
7	1	7		4		5	
8.89483	0.51993	8.99478	2.1893	8.79489	1.86776	8.89483	2.1683
9	4	1		8		9	
9.09472	0.83104	9.19466	2.15416	8.99478	2.17036	9.09472	2.17159
3	4	5		2		3	
9.29460	1.25254	9.39454	2.17777	9.19466	2.12999	9.29460	0.44661
7		9		6		7	
9.49449	1.69161	9.59443	2.17901	9.39455	2.13397	9.49449	0.42231
1		3				1	7
9.69437	2.14221	9.79431	2.1856	9.59443	2.12986	9.69437	0.41778
5		7		4		5	6
9.89425	2.16995	9.99420	0.42725	9.79431	2.12999	9.89425	0.67301
9		1		8		9	8
10.0941	2.16404	10.1940	0.42272	9.99420	0.44634	9.99420	0.84751
4		8	9	2		2	9
10.2940	2.15361	10.3939	0.45787	10.1940	0.42025	10.1940	1.28988
3		7	2	9		9	
10.4939	2.16047	10.5938	0.42904	10.3939	0.41915	10.3939	1.81463
1		5		7	9	7	
10.6938	2.15292	10.7937	0.52611	10.5938	0.48670	10.5938	2.1569

		4		5	8	5	
10.8936	0.42272	10.9936	0.87950	10.6938	0.61686	10.7937	2.17475
8		2	9		4	4	
11.0935	2.17818	11.1935	1.35153	10.8936	0.96601	10.9936	2.16802
6				8		2	
11.2934	-1.12417	11.3933	1.83371	11.0935	1.4383	11.1935	2.16734
5		9		6		1	
11.4933	0.42341	11.5932	2.1532	11.2934	1.92391	11.3933	2.16473
3		7		5		9	
11.6932	0.71626	11.7931	2.16226	11.4933	2.13837	11.5932	2.16734
2	5	6		3		7	
11.8931	1.07721	11.9930	2.16569	11.6932	2.15361	11.7931	0.41929
		4		2		6	
12.0929	1.49706	12.1929	2.15855	11.8931	2.15635	11.9930	0.41819
8		2				4	8
12.2928	1.93188	12.3928	2.16953	12.0929	2.12423	12.1929	0.42053
7		1		8		3	2
12.4927	2.1488	12.5926	2.16349	12.2928	0.49261	12.3928	0.47503
5		9		7		1	8
12.6926	2.144	12.7925	0.42753	12.4927	0.42327	12.4927	0.59077
4		8		5		5	8
12.8925	2.15265	12.9924	2.19878	12.6926	0.41737	12.6926	1.01049
2		6		4	4	4	
13.0924	2.1532	13.1923	2.19891	12.8925	0.42080	12.8925	1.44105
		4		2	7	2	
13.2922	2.15292	13.3922	0.41847	13.0924	0.52075	13.0924	1.92405
9		3			7		
13.4921	0.41957	13.5921	0.58405	13.1923	0.64761	13.2922	2.12876
7		1		5	8	9	
13.6920	0.64995	13.792	0.91671	13.3922	1.03108	13.4921	2.16418
6			6	3		7	
13.8919	0.61302	13.9918	1.34947	13.5921	1.48484	13.6920	2.15759
4		8		1		6	
14.0918	0.42300	14.1917	1.8046	13.792	1.96181	13.8919	2.15127
2	3	6				4	
14.2917	0.50977	14.3916	2.13466	13.9918	2.14413	14.0918	2.15072
1	4	5		8		2	
14.3916	0.64349	14.5915	2.15429	14.1917	2.15347	14.2917	2.15374
5	9	3		7		1	
14.5915	0.98935	14.7914	2.14345	14.3916	2.15663	14.4915	2.16445
3		2		5		9	
14.7914	1.40123	14.9913	2.14729	14.5915	2.15059	14.6914	2.16445
2				3		8	
14.9913	1.84442	15.1911	2.14674	14.7914	2.15004	14.8913	2.15086
		8		2		6	
15.1911	2.12148	15.3910	2.15031	14.9913	2.15059	15.0912	2.16075
9		7				4	
15.3910	2.11324	15.5909	2.15361	15.1911	2.15031	15.2911	2.15347

7	5	9	3
15.5909	2.17036 15.7908	2.17901 15.3910	2.14729 15.4910 2.15072
5	4	7	1
15.7908	2.13864 15.9907	2.18628 15.5909	2.144 15.6909 2.14976
4	2	5	
15.9907	2.13864 16.1906	0.49357 15.7908	2.13974 15.8907 2.15004
2		4	8
16.1906	2.13837 16.3904	0.46927 15.9907	2.14317 16.0906 2.151
1	9	2	6
16.3904	2.13837 16.5903	0.77708 16.1906	2.144 16.2905 2.15374
9	7	7	1
16.5903	2.13823 16.7902	1.18856 16.3904	2.15017 16.4904 2.15072
7	6	9	3
16.7902	2.13878 16.9901	1.6393 16.5903	2.1499 16.6903 2.15402
6	4	7	2
16.9901	2.14139 17.1900	2.08674 16.7902	2.15017 16.8902 2.15072
4	2	6	
17.1900	2.14125 17.3899	2.13782 16.9901	2.15086 17.0900 2.15457
3	1	4	8
17.3899	2.14166 17.5897	2.14743 17.1900	2.14743 17.2899 2.1569
1	9	3	7
17.5897	2.1418 17.7896	2.15773 17.3899	2.14715 17.4898 2.15388
9	8	1	5
17.7896	2.14166 17.9895	2.15182 17.5897	2.14688 17.6897 2.15361
8	6	9	4
17.9895	2.13892 18.1894	2.15457 17.7896	2.14702 17.8896 2.15004
6	4	8	2
18.1894	2.1385 18.3893	2.16253 17.9895	2.1499 18.0895 2.15704
5	3	6	

CF9T	CF9D	CF10T	CF10D	CF11T	CF11D	CF12T	CF12D
0	0.41861	0	2.18299	0	2.18148	0	0.42176
							8
0.19988	0.65063	0.19988	2.18285	0.19988	0.76157	0.19988	0.42877
4	8	4		4		4	
0.29982	0.83722	0.39976	2.18285	0.39976	0.54931	0.39976	0.76926
6	2	8		8		8	1
0.49971	1.30554	0.59965	2.18285	0.59965	0.50469	0.49971	1.01008
		2		2	4		
0.69959	1.86364	0.79953	0.43179	0.79953	0.51306	0.69959	1.62118
4		6		6	9	4	
0.89947	2.17022	0.99942	0.41888	0.89947	0.58748	0.89947	2.1775

1.09936 ⁸	2.16583	1.19930	0.41764	1.09936 ⁸	0.86729	1.09936 ³	2.17049 ⁸
2		4	9	2		2	
1.29924	2.16651	1.39918	0.45691	1.29924	1.31734	1.29924	2.17242
6		8	5	6		6	
1.49913	2.16638	1.49913	0.59338	1.49913	1.87037	1.49913	2.17255
			6				
1.69901	2.1661	1.69901	0.99868	1.69901	2.1764	1.69901	2.17283
4		4		4		4	
1.89889	2.16665	1.89889	1.51972	1.89889	2.16926	1.89889	2.1731
8		8		8		8	
2.09878	2.17049	2.09878	2.14674	2.09878	2.16926	2.09878	2.17324
2		2		2		2	
2.29866	0.41833	2.29866	2.18505	2.29866	2.1694	2.29866	0.42314
6		6		6		6	
2.49855	0.41668	2.49855	2.17338	2.49855	2.16926	2.49855	0.41723
	8						7
2.69843	0.4171	2.69843	2.17338	2.69843	2.1694	2.69843	0.41764
4		4		4		4	9
2.89831	0.53805	2.89831	2.17338	2.89831	0.43233	2.89831	0.51512
8	7	8		8		8	8
2.99826	0.70294	3.09820	2.17338	3.09820	0.42382	2.99826	0.68427
1	8	2		2	7	1	6
3.19814	1.14943	3.29808	2.17338	3.29808	0.41737	3.19814	1.15753
5		6		6	4	5	
3.39802	1.72223	3.49797	0.42437	3.49797	0.62441	3.39802	1.68159
9					5	9	
3.59791	2.16253	3.69785	0.41696	3.59791	0.79507	3.59791	2.15553
3		4	2	3	3	3	
3.79779	2.18697	3.89773	0.42327	3.79779	1.26682	3.79779	2.18848
7		8	8	7		7	
3.99768	2.18697	4.09762	0.55617	3.99768	1.85664	3.99768	2.16336
1		2	9	1		1	
4.19756	2.18519	4.19756	0.74235	4.19756	2.17708	4.19756	2.17077
5		5	1	5		5	
4.39744	2.18724	4.39744	1.23785	4.39744	2.16926	4.39744	2.1812
9		9		9		9	
4.59733	2.18738	4.59733	1.78607	4.59733	2.16239	4.59733	0.77763
3		3		3		3	
4.79721	2.18546	4.79721	2.15031	4.79721	2.17365	4.79721	0.43014
7		7		7		7	
4.99710	0.43028	4.99710	2.15924	4.99710	2.1764	4.99710	0.41819
1		1		1		1	8
5.19698	0.4171	5.19698	2.16706	5.19698	2.17777	5.19698	0.41874
5		5		5		5	7
5.39686	0.41902	5.39686	2.17708	5.39686	0.5467	5.39686	0.47229
9	2	9		9		9	2
5.49681	0.42739	5.59675	2.16596	5.59675	0.4403	5.49681	0.64720

1	7	3	3	1	6		
5.69669	0.69786	5.79663	2.16692	5.79663	0.4506	5.69669	1.05992
5	8	7	7	5			
5.89657	1.14106	5.99652	0.41957	5.99652	0.48657	5.89657	1.61363
9		1	1	1	9		
6.09646	1.6544	6.19640	0.41819	6.19640	0.78711	6.09646	2.14372
3		5	8	5		3	
6.29634	2.16185	6.39628	0.42108	6.39628	1.24856	6.29634	2.15539
7		9	1	9		7	
6.49623	2.16679	6.59617	0.51334	6.49623	1.52342	6.49623	2.15951
1		3	3	1		1	
6.69611	2.16583	6.69611	0.67054	6.69611	2.09773	6.69611	2.15539
5		5	6	5		5	
6.89599	2.16006	6.89599	1.09218	6.89599	2.15292	6.89599	2.15196
9		9		9		9	
7.09588	2.1499	7.09588	1.68145	7.09588	2.17708	7.09588	0.48396
3		3		3		3	
7.29576	2.1488	7.29576	2.18203	7.29576	2.1775	7.29576	0.41915
7		7		7		7	
7.49565	0.42492	7.49565	2.0818	7.49565	2.17708	7.49565	0.41861
1		1		1		1	
7.69553	0.41929	7.69553	2.07878	7.69553	2.17681	7.69553	0.41737
5	6	5		5		5	4
7.89541	0.41847	7.89541	2.08798	7.89541	0.4624	7.89541	0.41778
9	3	9		9		9	6
8.09530	0.42094	8.09530	2.16638	8.09530	0.42643	7.99536	0.45362
3	4	3		3		2	
8.19524	0.51636	8.29518	2.16651	8.29518	0.42574	8.19524	0.83543
6	4	7		7	9	6	8
8.39513	0.87003	8.49507	0.42396	8.49507	0.51430	8.39513	1.31927
	6	1		1	5		
8.59501	1.34975	8.69495	0.42272	8.59501	0.64418	8.59501	1.90936
4		5		4	6	4	
8.79489	1.91897	8.89483	0.42012	8.79489	1.07241	8.79489	2.1451
8		9		8		8	
8.99478	2.12148	9.09472	0.52034	8.99478	1.67692	8.99478	2.1591
2		3	5	2		2	
9.19466	2.13713	9.19466	0.71077	9.19466	2.1315	9.19466	2.15992
6		6	4	6		6	
9.39455	2.14647	9.39455	1.10769	9.39455	2.09636	9.39455	2.15649
9.59443	2.1532	9.59443	1.72113	9.59443	2.07343	9.59443	2.15992
4		4		4		4	
9.79431	2.15223	9.79431	2.11667	9.79431	2.18038	9.79431	0.45238
8		8		8		8	
9.99420	2.15704	9.99420	2.15361	9.99420	2.15237	9.99420	0.41723
2		2		2		2	7
10.1940	0.42341	10.1940	2.1488	10.1940	2.15196	10.1940	0.41929
9		9		9		9	6

10.3939	0.41806	10.3939	2.14935	10.3939	0.5062	10.2940	0.41998
7		7		7		3	3
10.5938	0.42423	10.5938	2.14963	10.5938	0.4587	10.4939	0.63622
5	9	5		5		1	2
10.7937	0.41902	10.7937	2.1558	10.7937	0.44620	10.6938	1.05511
4	2	4		4	6		
10.8936	0.44579	10.9936	2.15594	10.9936	0.55370	10.8936	1.61418
8	4	2		2	8	8	
11.0935	0.76898	11.1935	0.41833	11.0935	0.71475	11.0935	2.1385
6	7	1		6	5	6	
11.2934	1.22439	11.3933	0.41792	11.2934	1.17126	11.2934	2.11379
5		9		5		5	
11.4933	1.81119	11.5932	0.41819	11.4933	1.66923	11.4933	2.10885
3		7	8	3		3	
11.6932	2.12999	11.7931	0.46666	11.6932	2.1304	11.6932	2.13823
2		6	3	2		2	
11.8931	2.12134	11.9930	0.78793	11.8931	2.14523	11.8931	2.14139
		4	3				
12.0929	2.12175	12.1929	1.28014	12.0929	2.14798	12.0929	2.14564
8		3		8		8	
12.2928	2.13095	12.2928	1.53496	12.2928	2.13796	12.2928	0.4171
7		7		7		7	
12.4927	2.14839	12.4927	2.09883	12.4927	2.13796	12.4927	0.41984
5		5		5		5	6
12.6926	2.1234	12.6926	2.11352	12.6926	2.13809	12.6926	0.41806
4		4		4		4	1
12.8925	0.42712	12.8925	2.15828	12.8925	0.43179	12.8925	0.57210
2		2		2		2	6
13.0924	0.41819	13.0924	2.15072	13.0924	0.41888	12.9924	0.75347
	8					6	2
13.2922	0.41792	13.2922	2.14757	13.2922	0.41915	13.1923	1.23483
9	3	9		9	9	5	
13.4921	0.53544	13.4921	2.15127	13.4921	0.48739	13.3922	1.80955
7	8	7		7	5	3	
13.5921	0.68194	13.6920	2.14715	13.5921	0.61768	13.5921	2.1197
1	2	6		1	8	1	
13.792	1.12019	13.8919	0.42643	13.792	1.03767	13.792	2.11407
		4					
13.9918	1.66758	14.0918	0.42698	13.9918	1.59825	13.9918	2.16088
8		2		8		8	
14.1917	2.13782	14.2917	0.44153	14.1917	2.12629	14.1917	2.14921
7		1	8	7		7	
14.3916	2.16734	14.4915	0.41874	14.3916	2.05242	14.3916	2.14523
5		9	7	5		5	
14.5915	2.15965	14.6914	0.66052	14.5915	2.04707	14.5915	2.14153
3		8	4	3		3	
14.7914	2.15965	14.8913	1.12499	14.7914	2.0608	14.7914	2.14537
2		6		2		2	

14.9913	2.15347	15.0912	1.67664	14.9913	2.06011	14.9913	2.13878
		4					
15.1911	2.15594	15.2911	2.12299	15.1911	2.04871	15.1911	2.13933
9		3		9		9	
15.3910	2.15333	15.4910	2.10363	15.3910	2.05997	15.3910	2.13301
7		1		7		7	
15.5909	2.15663	15.6909	2.11201	15.5909	2.06437	15.5909	2.12944
5				5		5	
15.7908	2.15704	15.8907	2.11448	15.7908	2.06848	15.7908	2.14153
4		8		4		4	
15.9907	2.15731	16.0906	2.11228	15.9907	2.0678	15.9907	2.13864
2		6		2		2	
16.1906	2.15951	16.2905	2.11214	16.1906	2.0715	16.1906	2.1385
1		5		1		1	
16.3904	2.16294	16.4904	2.11214	16.3904	2.0748	16.3904	2.13233
9		3		9		9	
16.5903	2.16432	16.6903	2.11173	16.5903	2.0781	16.5903	2.13878
7		2		7		7	
16.7902	2.16665	16.8902	2.1116	16.7902	2.06766	16.7902	2.13823
6				6		6	
16.9901	2.1672	17.0900	2.10844	16.9901	2.06395	16.9901	2.13137
4		8		4		4	
17.1900	2.16734	17.2899	2.11201	17.1900	2.07535	17.1900	2.13494
3		7		3		3	
17.3899	2.1639	17.4898	2.11558	17.3899	2.0781	17.3899	2.13109
1		5		1		1	
17.5897	2.1639	17.6897	2.12409	17.5897	2.0748	17.5897	2.13109
9		4		9		9	
17.7896	2.15979	17.8896	2.11956	17.7896	2.0748	17.7896	2.13123
8		2		8		8	
17.9895	2.15773	18.0895	2.11558	17.9895	2.07576	17.9895	2.12738
6				6		6	

The following data was obtained with a stopwatch and not a CBR. It is for verification only.

15 Filters at from a height of 10 meters took 2.81 sec to reach the ground
 15 Filters at from a height of 5 meters took 1.44 sec to reach the ground

COFFEE FILTER TERMINAL VELOCITY

TI-83 PROGRAM “TERMVEL”

This is the Coffee Filter Terminal Velocity assessment program for the TI-83 Plus or TI-83 It can be copied and pasted in the Graph Link Program to a new TI-83 Program File then linked to the TI-83 Plus or TI-83 either directly or using TI CONNECT. Download free

TI CONNECT

<http://education.ti.com/us/product/accessory/connectivity/down/download.html>

TI-GRAPH LINK

<http://education.ti.com/us/product/accessory/connectivity/down/downgraph.html>

This program reads correctly with the TI83Pluspc Font, which is loaded with the TI-83Plus GRAPH LINK Program. We have experienced some difficulty with the list name L,, , which when copied from here and pasted into TI-Graph Link comes out L" rather than L,, . These items have been highlighted and are most easily corrected before saving in TI-Graph Link.

You will need to give this a name. We used TERMVEL.
COPY AND PASTE EVERYTHING BETWEEN THESE LINES

```
ExprOff
AxesOff
Simul
FnOff
PlotsOff
ClrHome
ClrDraw
Text(1,1,"DROPS DONE"
StorePic 3
ClrDraw
Output(1,1," A PROGRAM FOR")
Output(2,1," PROCESSING")
Output(3,1," COFFEE FILTER")
Output(4,1," VELOCITY")
Output(5,1," W. CAUDILL")
Output(6,1," S. PARKER")
Output(7,1," MEOVSD MPCC")
Output(8,1,"ZANESVILLE OHIO")
Pause
ClrHome
Output(1,1,"THIS PROGRAM WILL")
Output(2,1," SAVE ORIGINAL")
Output(3,1," DATA IN L...,L†")
```

```

Output(4,1,"THEN LISTS L_-L„")
Output(5,1,"WILL BE USED FOR")
Output(6,1,"PROCESSING")
Pause
ClrHome
Input "TIME LIST =",L...
Input "DISTANCE LIST =",L†
Output(6,1,"IN THIS DROP?")
Input "NØ. OF FLTRS =",R
ClrList L_,L,,Lf,L„
ú.05üXmin
18üXmax
ú.05üYmin
2.5üYmax
PlotsOff
FnOff
{13,7}üdim([A])
{13,7}üdim([B])
ClrHome
Plot2(xyLine,L...,L†,Ø)
Text(0,0,"LOOK OVER THE GRAPH")
Text(57,0,"SMOOTHING NEEDED ANYWHERE?")
Pause
ClrHome
ØüS
Menu("IS SMOOTH NEEDED","NO",6,"YES",5
Lbl 5
1üS
Lbl 6
1+SüS
Lbl 7
ClrHome
PlotsOff
FnOff
ú.05üXmin
18üXmax
ú.05üYmin
2.5üYmax
Plot2(xyLine,L...,L†,Ø)
PlotsOn 2
For(X,Ø,9)
Text(25,5X,X)

```

```

End
For(X,0,8)
Text(25,5X+51,X)
End
Text(57,0,"NOTE START TIME OF DROP")
RecallPic 3
For(Z,1,6)
If [A](R,Z)>0
Text(1,35+5Z,Z)
End
StorePic 3
Pause
ClrHome
Input ("DROP NUMBER?",C)
Input ("START TIME?",T)
ClrHome
Output(3,1,"PLEASE WAIT")
TüXmin
T+3.5üXmax
ú.25üYmin
2.7üYmax
L...üL_
L†üL,
SortD(L_,L,)
1üP
While T<L_(P)
L_(P)üLf(P)
L,(P)üL,,(P)
P+1üP
End
SortA(Lf,L,,)
If S=1
Goto 2
Lbl 1
ClrHome
Plot2(xyLine,Lf,L,,_)
PlotsOn 2
Text(0,0,"SMTHNG NEEDED PRESS ZERO")
Text(57,0,"NONE NEEDED PRESS ENTER")
0üK
While K=0
getKeyüK

```

```

End
If K=102
Goto 3
If K=105
Goto 2
Goto 1
Lbl 3
Plot2(xyLine,Lf,L,,_)
Text(0,0,"SELECT THE WAY-OUT PART")
Trace
For(E,1,100)
If Lf(E)=X
Then
0üLf(E)
0üL,,(E)
100üE
End
End
SortA(Lf,L,,)
Goto 1
Lbl 2
ClrHome
Plot2(xyLine,Lf,L,,_)
Text(0,0,"SELECT LINEAR PART")
Select(L_,L,)
LinReg(ax+b) L_,L,,Y_
aü[A](R,C)
ClrHome
FnOff
Plot2(xyLine,Lf,L,,_)
Text(0,0,"SELECT PARABOLIC PART")
Select(L_,L,)
PlotsOff
QuadReg L_,L,
ClrList áMIN
For(J,1,40)
L_(2)-.01*JüX
aXÜ+bX+cüáMIN(J)
End
min(áMIN)üL
([A](R,C)-b)Ü/(4*a)+b([A](R,C)-b)/(2*a)+c-LüD
Dü[B](R,C)

```

```

0üW
0üG
0üH
0üM
For (V,1,6)
If ([A](R,V)>0)
Then
W+[A](R,V)üW
H+1üH
End
If ([B](R,V)>0)
Then
M+[B](R,V)üM
G+1üG
End
End
W/Hü[A](R,7)
M/Gü[B](R,7)
ClrHome
Float
Disp R
Fix 2
Disp [A](R,C),[A](R,7),[B](R,C),[B](R,7)
Output(1,1,"NUMBER OF CF")
Output(2,1,"TREMVEL NOW")
Output(3,1,"AVG TERMVEL")
Output(4,1,"THIS DROP")
Output(5,1,"AVG DROP")
Output(7,1,"PRESS ENTER")
Float
Pause
ClrHome
FnOff
Menu("DO ANOTHER DROP?","YES",7,"NO",8
Lbl 8
AxesOn
ExprOn
Stop

```

COFFEE FILTER TERMINAL VELOCITY

CONCLUSION

We have analyzed the collected data by hand and by use of the assisting program and should now have enough information to draw some reasonable conclusions. We will fill out this table with our collected data.

Number of Filters L1				Average L2
1				
2				
3				
4				
5				
6				
7				
8				
9				
10				
15				3.6496

Now we will put this data in a list and display it to see if some conclusion can be reached,

Press **GRAPH** **ENTER**

Scroll to the top of L1 Press **CLEAR** **ENTER**

Then enter the number of filters that go with our data above.

Scroll to the top of L2 Press **CLEAR** **ENTER**

Then enter the terminal velocity of the filters from our data above keeping the number of filters in L1 lined up with the data in L2.

Press

2nd

STAT PLOT

Then Press

ENTER

```
5:Hi-LoE
1:Plot1...On
  L1  L2  .
2:Plot2...Off
  L1  L2  □
3:Plot3...Off
  L1  L2  □
4↓PlotsOff
```

becomes

```
Plot1 Plot2 Plot3
Off Off
Type: [ ] [ ] [ ]
      [ ] [ ] [ ]
Xlist:L1
Ylist:L2
Mark: [ ] + .
```

but it may not look like this. Move the cursor to highlight an item

Then Press

ENTER

highlight **On** , not connected



dots

, make **Xlist:L1** and

Ylist:L2

and highlight the box dot



Press

Y=

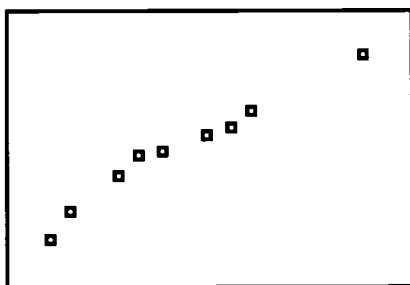
```
Plot1 Plot2 Plot3
\Y1=
\Y2=
\Y3=
\Y4=
\Y5=
\Y6=
\Y7=
```

By highlighting and clearing
make the screen look like this

Press

ZOOM

9



If we have enough data we may get something like this. We said in the beginning that the terminal velocity was proportional to the square root of the number of filters and hoped to show that.

$$V_{\text{terminal coffee filter}} = K \sqrt{N} \quad \text{Where} \quad K = \sqrt{\frac{Mg}{P}}$$

For regular 8-12 cup size, not heavy-duty industrial commercial grade, but the kind you get at K-Mart or WalMart, any brand. We have found that

$$K \cup 1 \quad \text{and so} \quad V_{\text{terminal coffee filter}} = \sqrt{N}$$

In this exercise have attempted to verify this item.

The data for 15 coffee filter terminal velocity came from use of our school's Power Lineman Program's bucket truck. We dropped 15 filters from 10 meters and timed the drop with a stopwatch. Then dropped from 5 meters and timed the drop. This gave us the time for the first 5 meters for both drops and left the time for the last 5 meters of the 10 meter drop at terminal velocity..

When many drops have been processed the above graph is even more convincing. Data from the seventh column of matrix A can be transfered to a list with built-in commands.

Press 2nd MATRIX

Scroll over to Math Down to 8:Matr>list Press ENTER

This is pasted to the home screen and with these arguments will put the processed data in the right place.

Press ENTER

```
Matr>list([A],7,
L2)
```

To complete the transfer

Press STAT ENTER

Scroll to the top of L1 Press CLEAR ENTER

Then enter the number of filters that go with non-zero data.

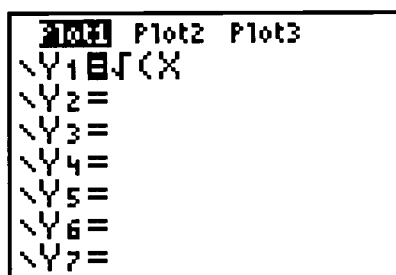
Delete entries that are zero in both L1 and L2.

Add the data from the 15 filter drop (3.6496)

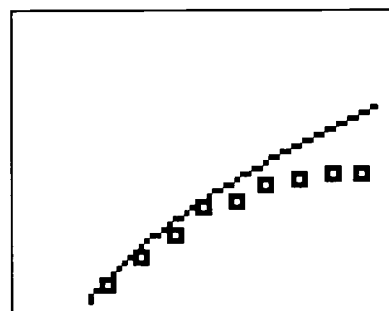
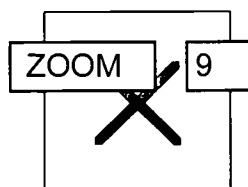
Press Y=

Enter

$$Y_1 = \sqrt{X}$$



Press



Actually our data looks more like $K = .9$ with more deviation at higher numbers of filters.

The data from many drops provided a similar plot for distance of fall before reaching terminal velocity. It turned out to be inconclusive for us. This is an area your student may find interesting. The use of different collection time periods in the CBR may be somewhat productive for refining this data.

The use of the velocity and acceleration plots with the CBR was not at all worthwhile for us but leaves other good material for student investigation.

Teach well.



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